

MTH4100 Exercise sheet 7

Calculus 1, Autumn 2008 Rainer Klages

- Make sure you attend the excercise class that you have been assigned to!
- The instructor will present the starred problem in class.
- You should then work on the other problems on your own.
- The instructor and helper will be available for questions.
- Solutions will be available online after the exercise class took place.

Strategy for Graphing y = f(x)

- 1. Identify the domain of f and any symmetries the curve may have.
- **2.** Find y' and y''.
- 3. Find the critical points of f, and identify the function's behavior at each one.
- 4. Find where the curve is increasing and where it is decreasing.
- 5. Find the points of inflection, if any occur, and determine the concavity of the curve.
- 6. Identify any asymptotes.
- 7. Plot key points, such as the intercepts and the points found in Steps 3–5, and sketch the curve.
- (*)1. Curve sketching.

Sketch the graph of

$$f(x) = \frac{12}{3+x^2}$$

by following step by step the strategy for graphing given above.

2. Curve sketching.

Sketch the graph of

$$f(x) = \frac{x}{1+x^2}$$

by following step by step the strategy for graphing given above.

Extra: The sum of two non-negative numbers is 20. Find the numbers if the product of one number and the square root of the other is to be as large as possible.

[2007 exam question]

[2008 exam question]