

MTH4100 Exercise sheet 1 Calculus 1, Fall 2008 Rainer Klages

- Make sure you attend the excercise class that you have been assigned to!
- The instructor will present the starred problems in class.
- You should then work on the other problems on your own.
- The instructor and helper will be available for questions.
- Solutions will be available online after the exercise class took place.
- (\*)1. Determine the set of all real numbers  $x \in \mathbb{R}$  that satisfy

$$x^2 - 3x - 4 < 0$$

- (a) by solving the inequality, and
- (b) by plotting the graph of  $y = x^2 3x 4$ .
- 2. Determine the set of all real numbers  $x \in \mathbb{R}$  that satisfy

$$|2x - 1| + |4x + 1| < 3$$

(\*)(a) by solving the inequality (instructor will give you some hints), and (b) by plotting the graph of y = |2x - 1| + |4x + 1|.

3. Determine the set of all real numbers  $x \in \mathbb{R}$  that satisfy

$$\sqrt{1-x^2} \le -x$$

(a) by solving the inequality, and

(b) by plotting the graphs of y = -x and  $y = \sqrt{1 - x^2}$ .

Extra: Prove that for all positive real numbers  $x, y \in \mathbb{R}^+$ 

$$\frac{2}{\frac{1}{x} + \frac{1}{y}} \le \sqrt{xy}$$

(a) by direct proof, and

(b) by using the arithmetic-geometric inequality.