

# Optimal design for TGF beta RI kinase inhibitor

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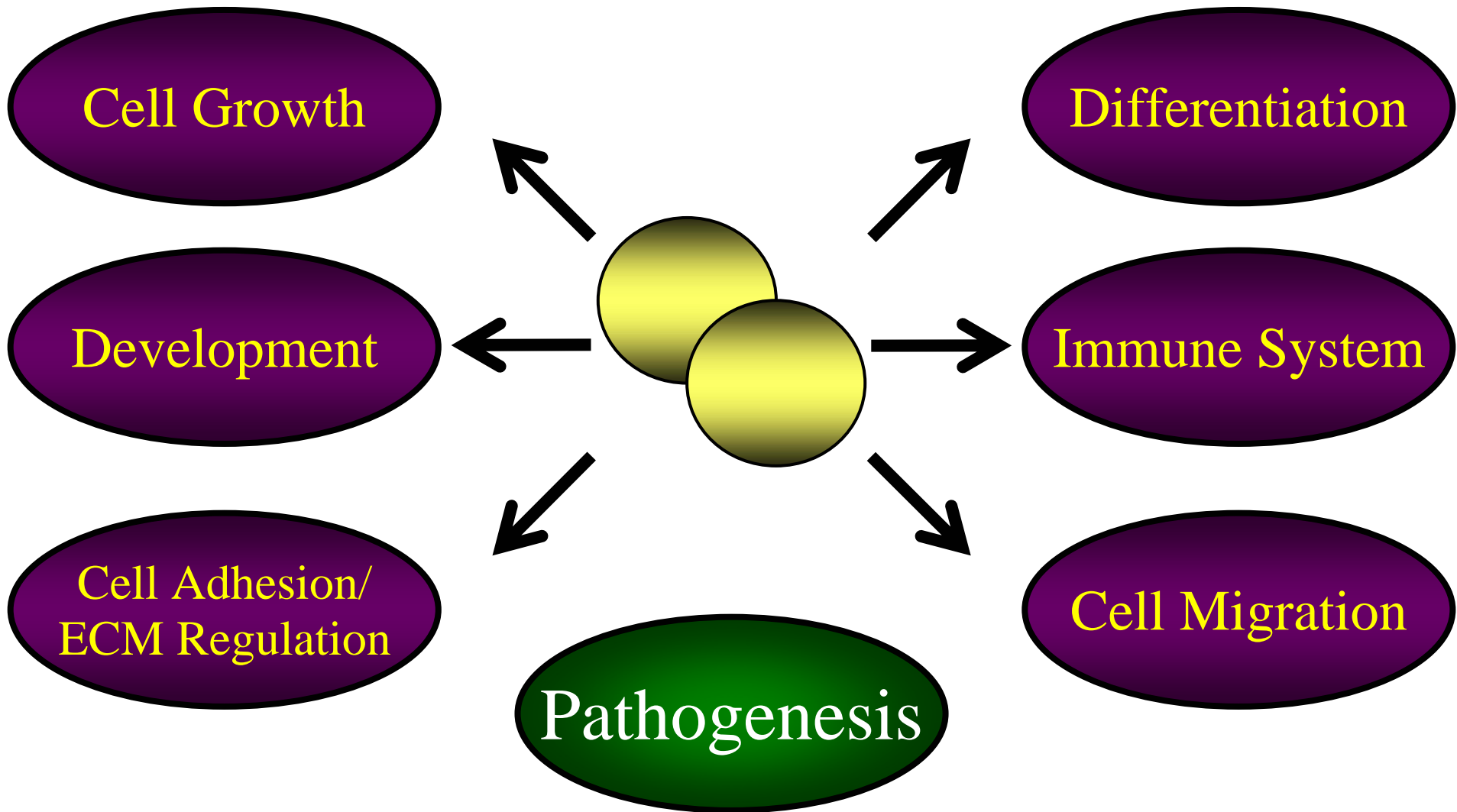
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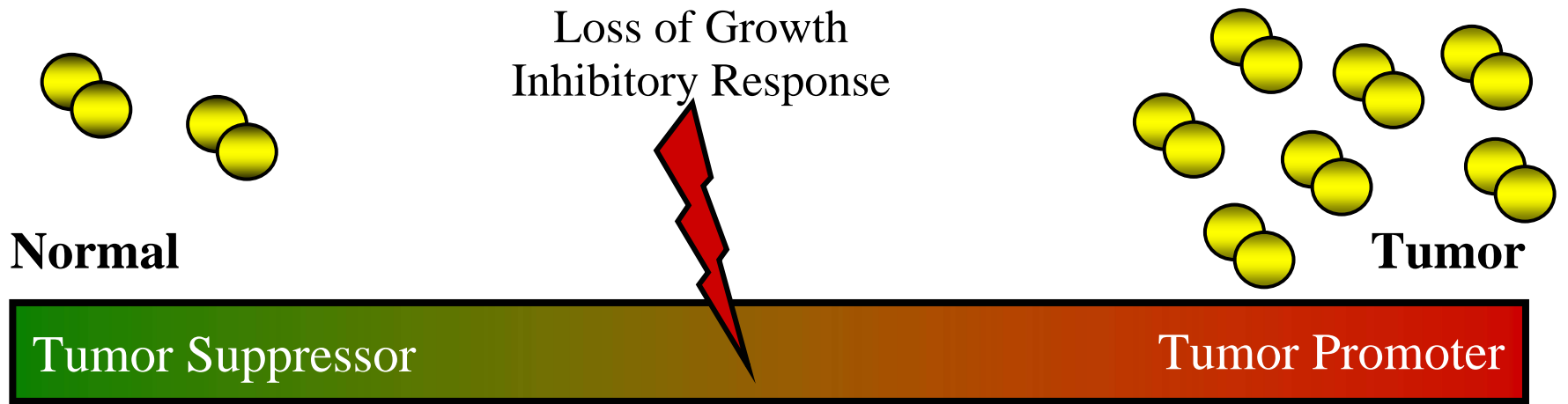
MANCHESTER  
1824

*Lilly*  
Answers That Matter.

# Outline

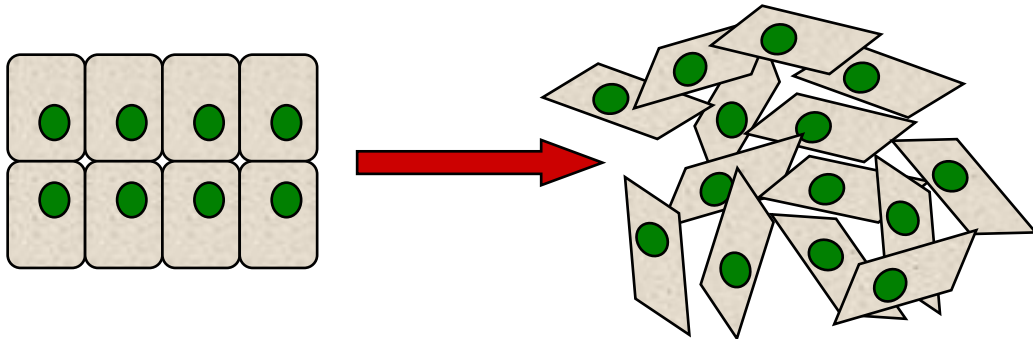
- Background
- Strategy
- TGFb PK/PD model in rats
- Multivariate optimal design
- TGFb PK/PD model & design  
in human
- Challenges in optimal design from practical  
point of view





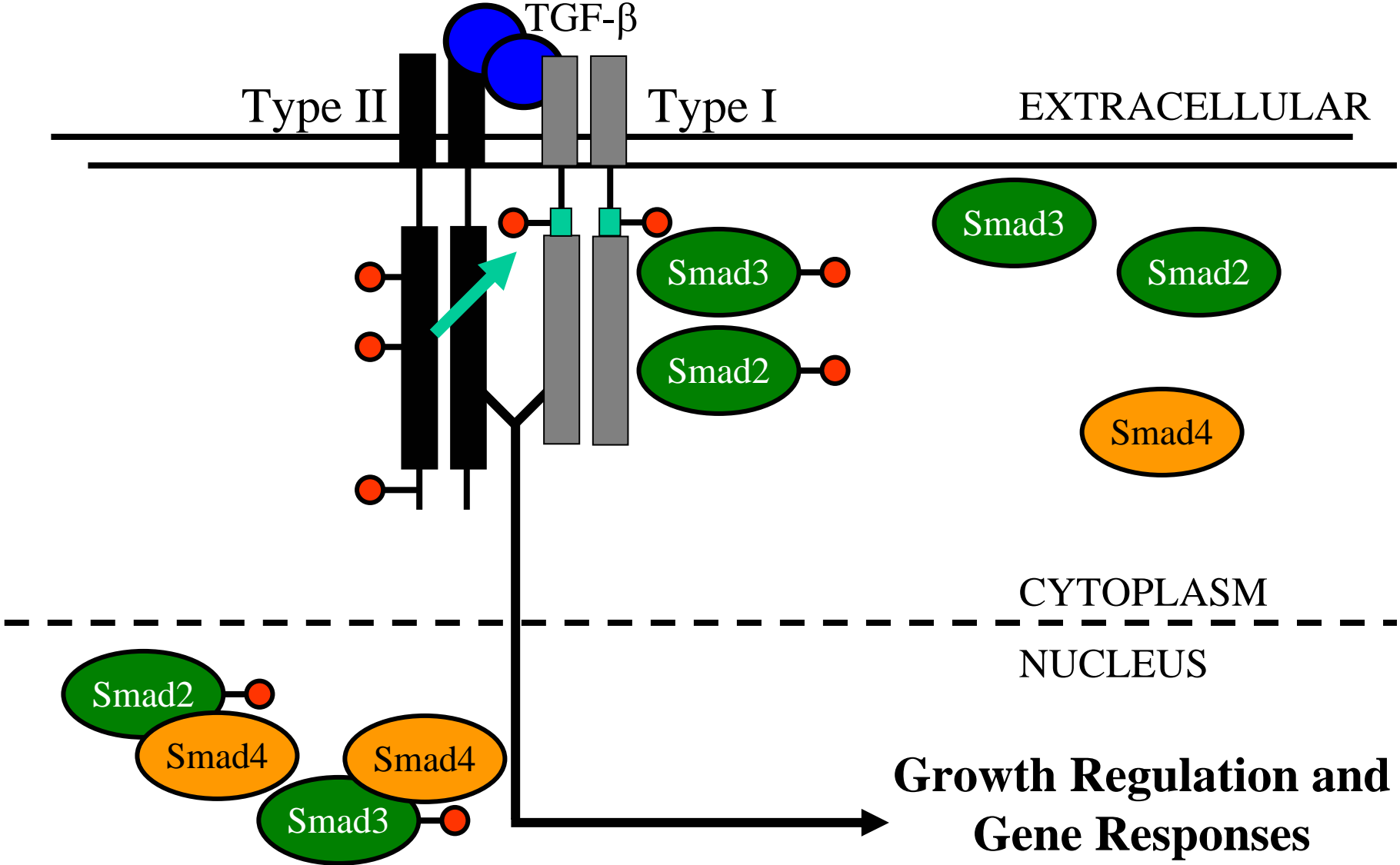
Tumor Cell

- Epithelial-to-mesenchymal transition
- Increased cell motility and invasiveness



Tumor Microenvironment

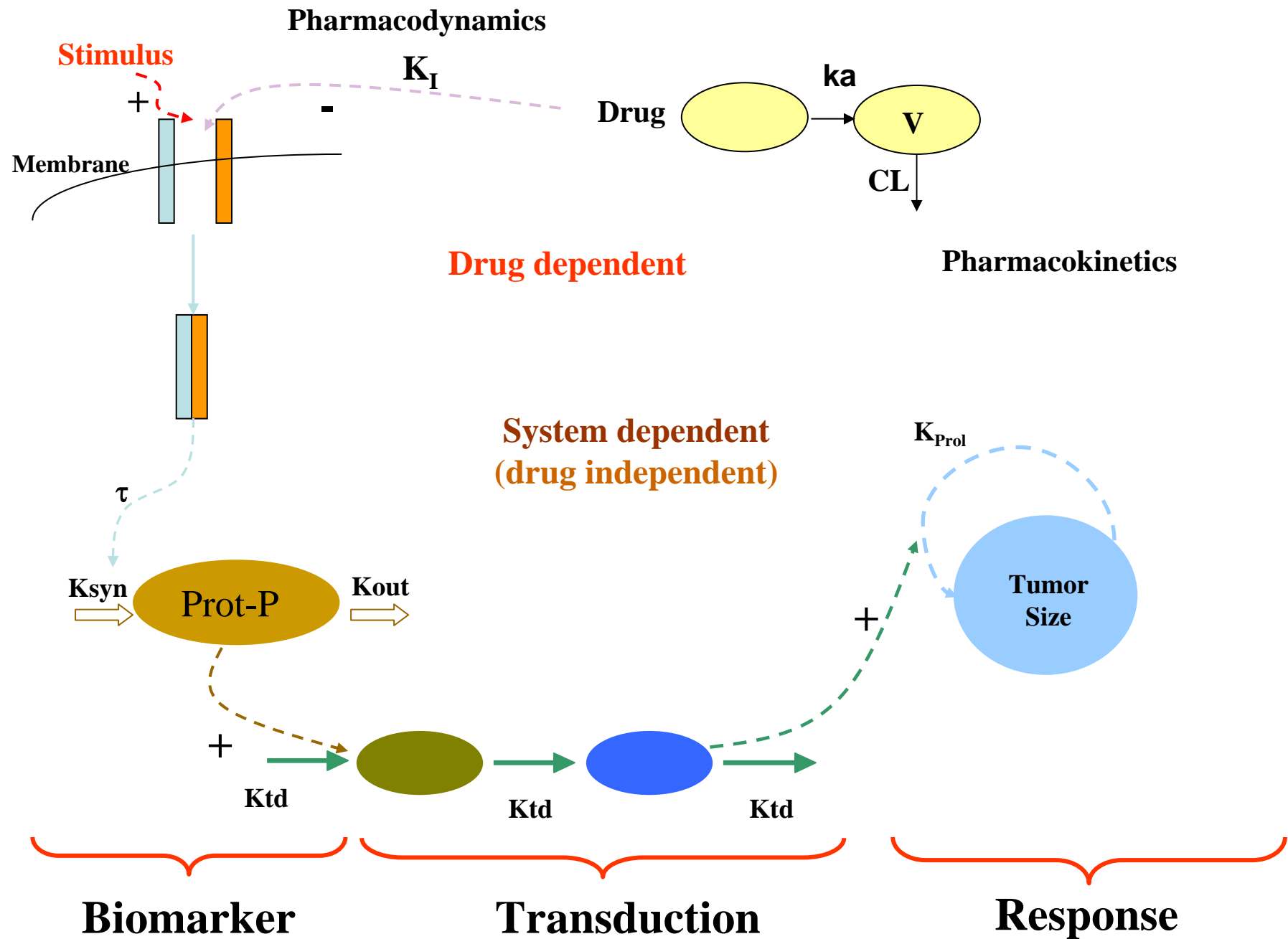
- Extracellular matrix remodeling
- Activated stromal cells
- Protease activation
- Angiogenesis
- Immunosuppression



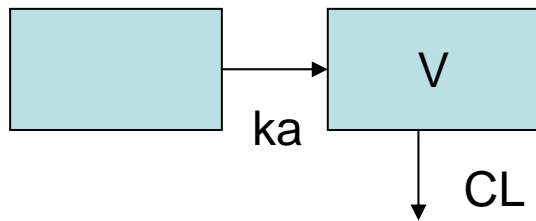
# **Understand PK and determine PKPD relationship in animals:**

## **Assist appropriate dose range selection**

- Develop PK/PD model in animals using Smad phosphorylation (biomarker)
  - In rats, mouse
- Perform allometric scaling to predict human PK
- Variability of biomarker has been incorporated to assess response variability



# Rat Pharmacokinetics



$$y_{ij} = f(\theta_i, t_{ij}) + \varepsilon_{ij}$$

$$\theta_i = \theta + b_i \quad \theta_i = \theta \exp(b_i) \quad b_i \sim N(0, \Omega)$$

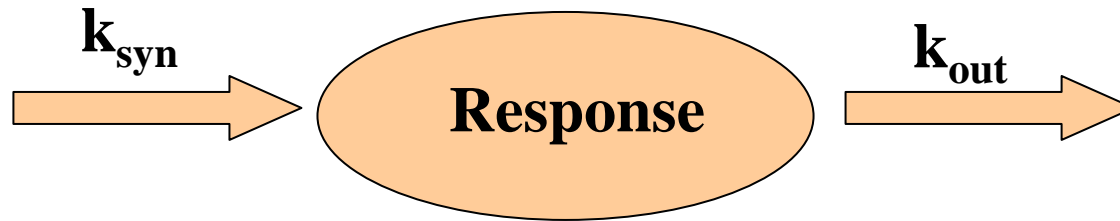
$$\xi_i = [t_{i1}, \dots, t_{in}]$$

	Parameters	Estimates	95% CI
<b>Disposition</b>	V (L)	1.09	[0.76 ; 1.42]
	CL (L/h)	0.339	[0.23 ; 0.45]
<b>Absorption</b>	KA (h <sup>-1</sup> ) fixed	8.00	
	F (%)	0.65	[0.49 ; 0.81]
<b>Interanimal variability</b>	$\omega^2_{CL}$	0.48 (CV=69.6%)	[0.245 ; 0.723]
	$\omega^2_V$	0.64 (CV=80.1%)	[0.335 ; 0.947]
<b>residual error: additive part</b>	$\mu\text{mol/L}$	64.20	[0.33 ; 0.95]



# Indirect Response Models

- Baseline response is maintained by factors controlling response synthesis and degradation

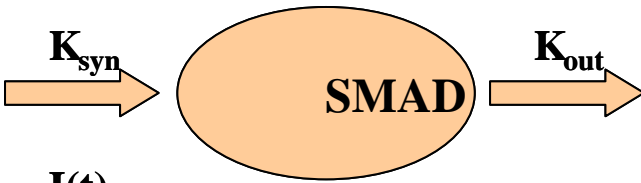


$k_{\text{syn}}$  is a 0 order rate constant

$k_{\text{out}}$  is a 1<sup>st</sup> order rate constant

$$\frac{dR}{dt} = k_{\text{syn}} - k_{\text{out}} * R$$

# Summary of PD parameters corresponding to biomarker model (mice)



$$I(t) = 1 - \frac{I_{\max} \times C^\gamma}{C^\gamma + IC_{50}^\gamma}$$

$$k_{\text{syn}} = k_{\text{out}} \times p\text{SMAD}(\%)$$

$$p\text{SMAD} = 100(\text{fixed})$$

Parameter	Population mean Estimate (%SEE) MX1	Population mean Estimate (%SEE) Calu6
$K_{\text{out}} (\text{h}^{-1})$	1.3 (15.8)	2.2 (6.9)
$I_{\text{MAX}}$	1*	1*
$IC_{50} (\mu\text{M})$	0.7 (11.2)	0.8 (7.6)
<b>n</b>	2.5 (17.4)	1*
<b>Additive Residual error (SEE %)</b>	10.6% (28.6)	18.4% (11.9)

SEE Standard error of the estimate

\* Fixed

Calu6: Lung cancer cell line;  
MXI: Brest cancer cell line.

$t_{1/2\_k\text{out}}(\text{MX1})=32 \text{ min}$

$t_{1/2\_k\text{out}}(\text{Calu6})=18.6 \text{ min}$

# Summary of PD parameters corresponding to biomarker model (rats)

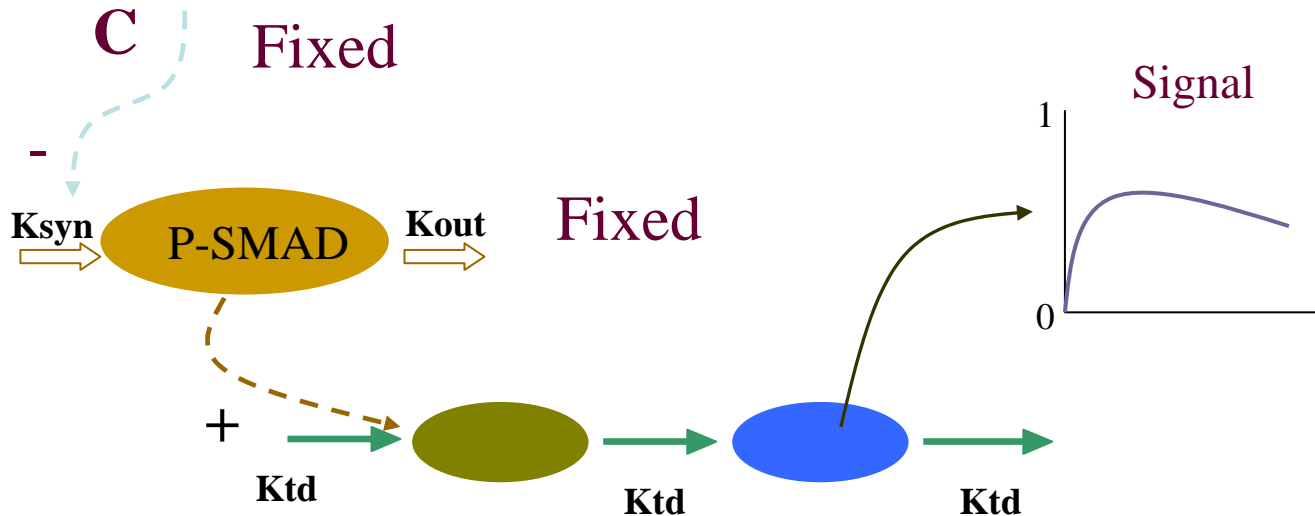
Parameter	Population mean Estimate (%SEE) Tumor		Population mean Estimate (%SEE) PBMC	
	$K_{out}$ ( $h^{-1}$ )	36.7	(7.3)	47.4
$I_{MAX}$	0.86	(3.4)	0.95	(1.1)
$IC_{50}$ ( $\mu M$ )	0.72	(25.7)	1.96	(13.1)
<b>Proportional Residual error (SEE %)</b>	62.1%	(19.9)	70.2%	(25.2)

SEE Standard error on the estimate

PBMC: peripheral blood mononuclear cell

# Semi-mechanistic model for tumor growth delay

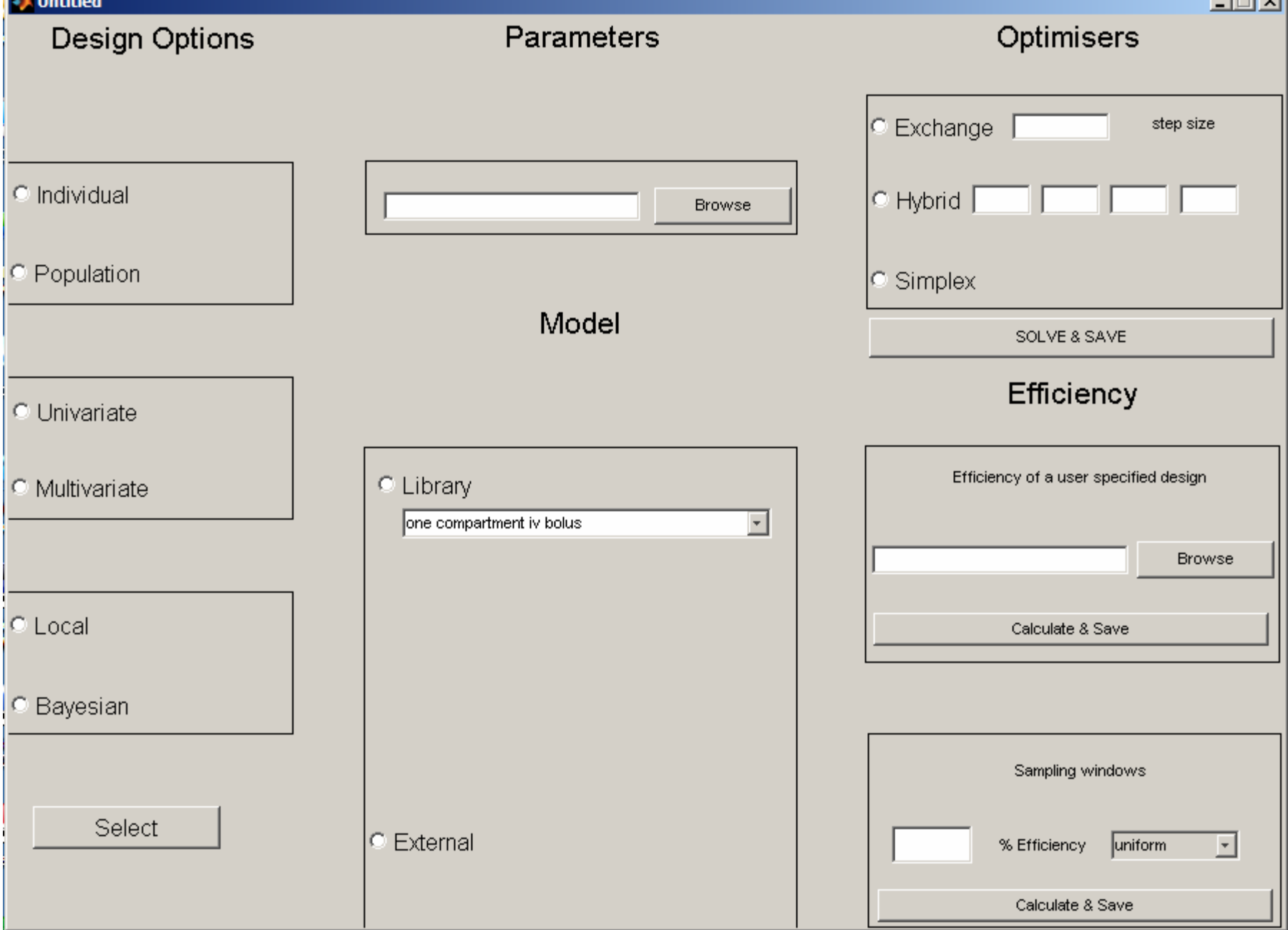
$$\frac{dTS}{dt} = \frac{K_{grw1} \times TS}{\left[ 1 + \left( \frac{K_{grw1}}{K_{grw0}} \times TS \right)^\gamma \right]^{1/\gamma}} \times (1 - I(t))$$



# **Retrospective optimal design in rats**

# TGF-beta inhibitor pharmacokinetic/pharmacodynamic parameters in rats

	Parameter name	Individual RAT	Population RAT mean [%SEE]
<b>Pharmacokinetic</b>	$k_a$ [ $h^{-1}$ ]	10	8
	V [L]	0.85	0.9 [15.5]
	CL [L/h]	0.29	0.34 [16.6]
	F [%]	65.3	65 [0.1]
	$\omega_{CL}^2$	----	0.48 [2.5]
	$\omega_v^2$	----	0.64 [24.3]
	Additive residual error $\sigma_{PK\_ADD}^2$	64.2	64 [32.9]
<b>Pharmacodynamic</b>	$k_{out}$	36.7	36.7 [7.3]
	$I_{max}$	0.86	0.86 [3.4]
	IC50	0.72	0.72 [25.7]
	Proportional residual error $\sigma_{PD\_PROP}^2$ [%]	62	62[19.9]



# Rat design constraints

- Individual rat

- PK model  $y_j = f(\theta, t_j) + \varepsilon_j$

- Three sampling times (j=3)
    - Time bounds (0-24h)

- PK/PD model  $y_{mj} = f_m(\theta, t_j) + \varepsilon_{mj}$

- Six sampling times chosen
    - Number of responses (M=2)
    - Response covariance matrix
    - Time bounds (0-24h)

$$\Sigma = \begin{pmatrix} 1 & 0.15 \\ 0.15 & 1 \end{pmatrix}$$



# Rat design constraints

- Population rat

- PK model  $y_{ij} = f(\theta_i, t_{ij}) + \varepsilon_{ij}$

- Three sampling times (j=3)
    - Time bounds (0-24h)

- PK/PD model  $y_{imj} = f_m(\theta_i, t_{ij}) + \varepsilon_{imj}$

- Six sampling times chosen
    - Number of responses (M=2)
    - Response covariance matrix
    - Time bounds (0-24h)

$$\Sigma = \begin{pmatrix} 1 & 0.15 \\ 0.15 & 1 \end{pmatrix}$$

# Optimal design for rat individual and rat population TGFb model

Optimiser	Optimal sampling times (h)									
Individual PK	0.1	0.5	3.46							
Individual PK/PD	0.0	0.0	0.5	0.5	3.5	24.0				
Population PK	0.1	1.0	7.1							
Population PK/PD	0.0	0.5	1.75	7.5	18.75	24				
CVSE <sup>a</sup> [%]										
	<b>ka</b>	<b>CL</b>	<b>V</b>	$\omega^2_{CL}$	$\omega^2_V$	$\sigma_{PK_2ADD}$	<b>Imax</b>	<b>IC50</b>	<b>kout</b>	$\sigma_{PD_2PROP}$
Individual PK	0.43	0.32	0.16	--	--	40.83				
Individual PK/PD	0.30	0.31	0.12	--	--	28.9	20.6	244.6	35.7	126.9
Population PK	0.12	13.5	13.5	45.4	45.4	18.3				
Population PK/PD	0.10	12.4	12.4	33.2	36.0	9.13	1.66	18.8	4.24	11.75

\* In all cases Exchange algorithm (Ogungbenro, 2006, Computer Method Prog Biomed) with 0.01 step size was used

# Optimal design for individual and population TGFb model

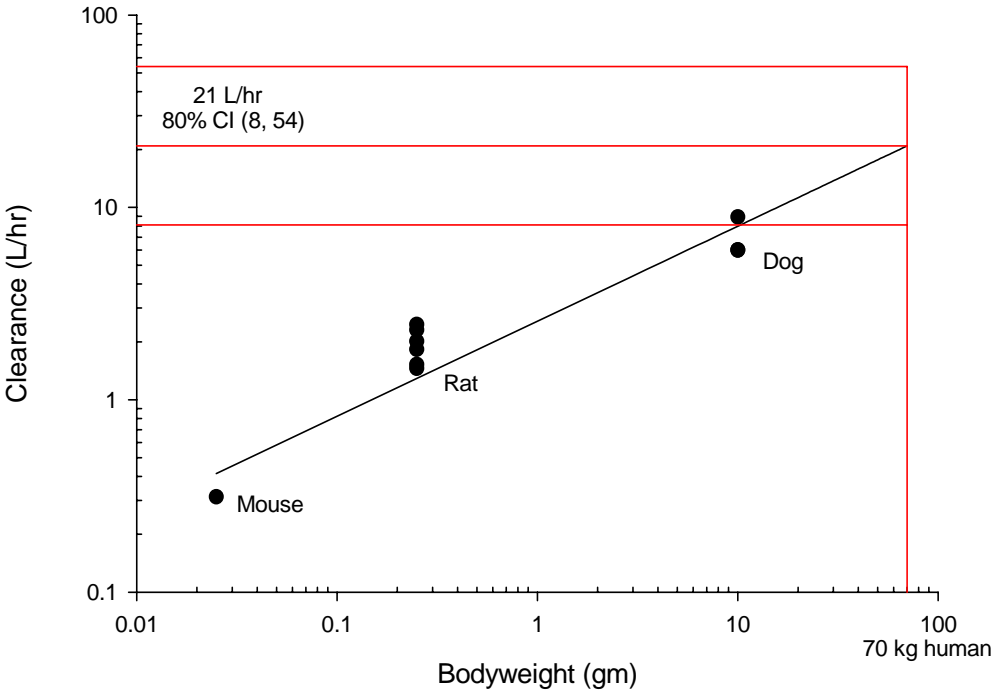
- Individual rat
  - PK
    - Early sampling with last time at 3.5h (due to additive model)
    - small CVSE on structural parameters; larger on additive error (40%);
  - PK/PD:
    - Last sampling at the upper bound (p-SMAD proportional error) and repeating the two early times;
    - Parameter CVSEs <40 with exception of IC50;
- Population rat
  - PK
    - Later last time point (7h)
    - CVSEs < or around 40%
  - PK/PD
    - No repeating time points with more even distribution in time (i.e. requiring samples before and after 12h);
    - Lower CVSEs (compared with individual PK/PD) < or around 30%.

# Interspecies allometry

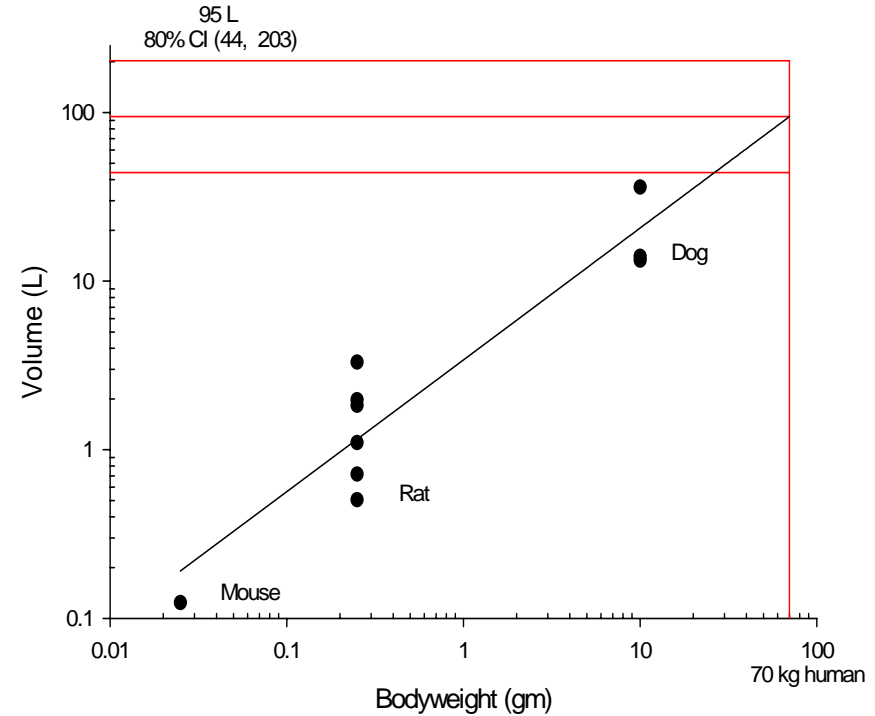
- Using IV PK parameters in rat, mouse and dogs
- Included in the model was an allowance for estimating correlation between animals within a species
- Human clearance predicted to be 20.9 L/h (8.11-53.76).
- Volume of distribution predicted to be 94.57L (44.13-202.69).
- Assumed bioavailability 50% (biopharmaceutics)

# Allometric scaling

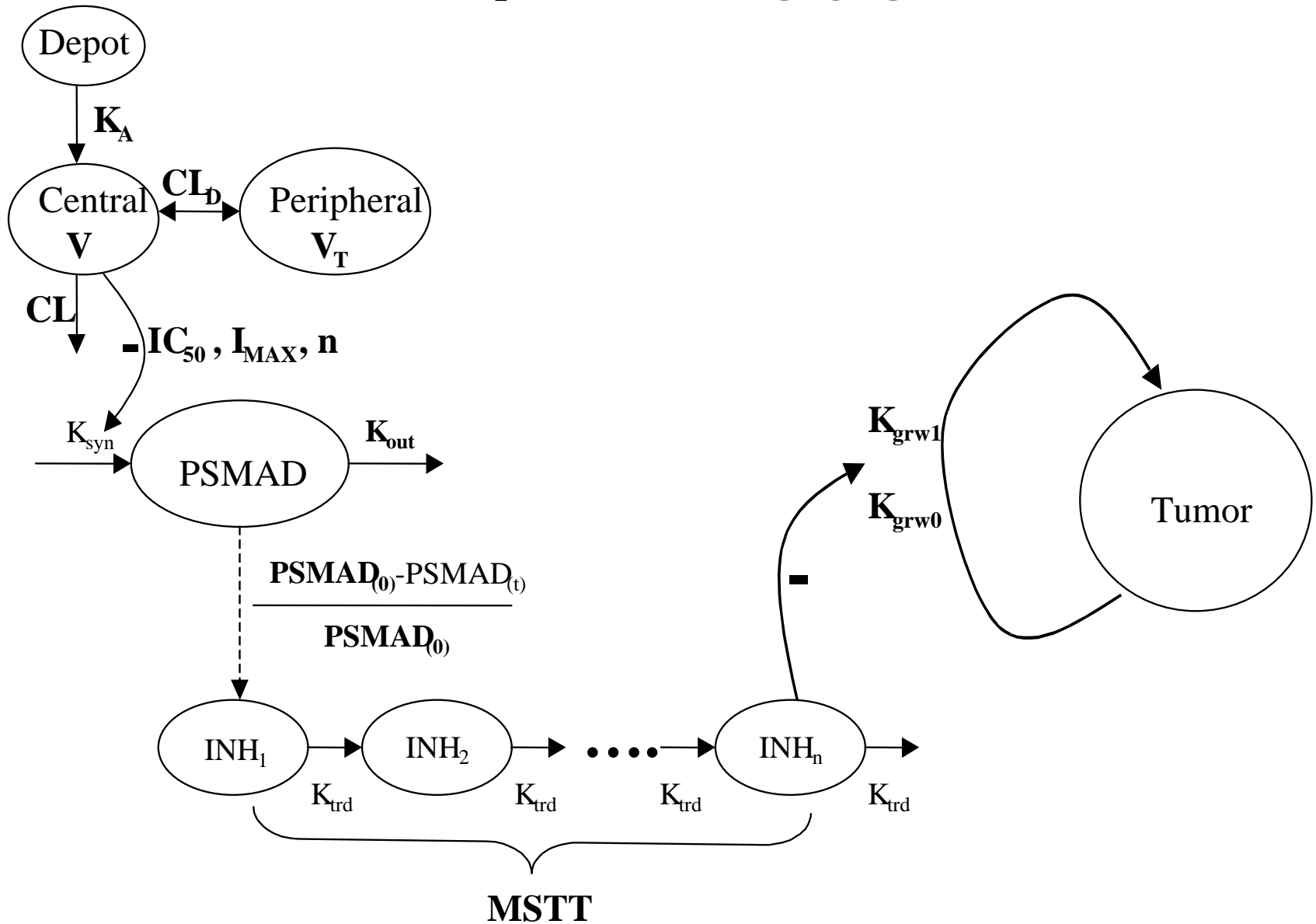
Allometric scaling for Clearance (L/hr)



Allometric scaling for Volume (L)



# PK/PD model



# Design first in human studies

- Based on simulations
- Based on D-optimal design

# Simulations in humans

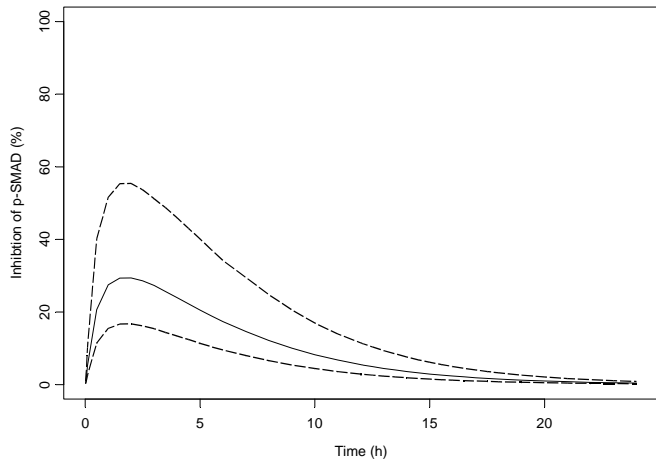
- Preclinical data suggest that
  - 30% inhibition of pSMAD over 24 hours and at least 50% inhibition at  $t_{max}$  ( time at maximum inhibition) is required for tumor growth delay
- Simulation in humans were performed in order to achieve this level of inhibition
- Simulation used both cell lines, used allometric scaling for PK using mouse, rat and dog.
- Variability of the biomarker was incorporated in the simulations



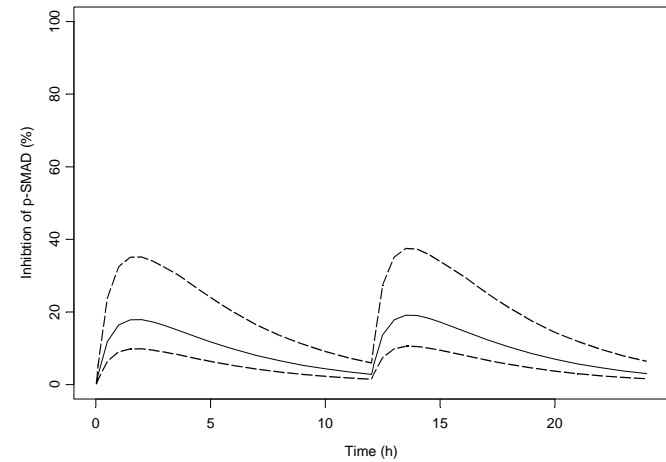
# From rat model :

## Simulated human PD and 90%CI profiles after QD and BID administrations

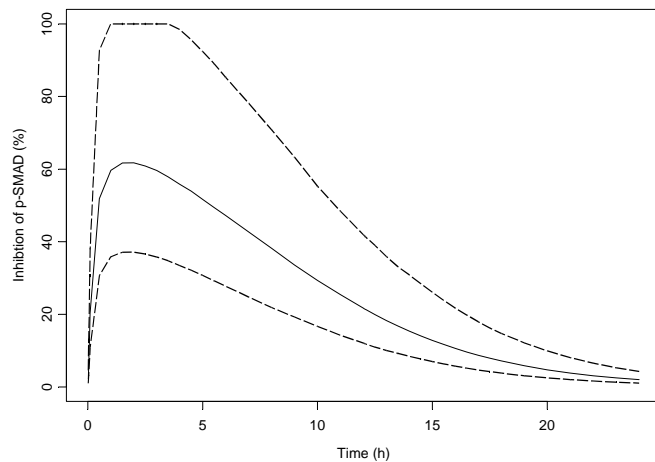
LY2157299:after administration of QD Amg



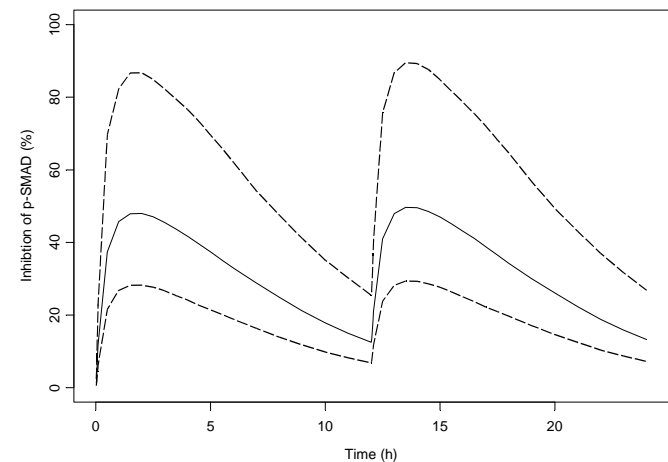
LY2157299:after administration of BID Amg



LY2157299:after administration of QD Bmg



LY2157299:after administration of BID Bmg



# D-optimal design in human

Design	Optimal sampling times (h)								
<b>Individual PK</b>	0.0	0.75	24.0						
<b>Individual PK/PD</b>	0.0	0.0	0.8	0.8	24	24			
<b>CVSE<sup>a</sup> [%]</b>									
	ka	CL	V	Imax	IC50	kout	$\sigma_{PK\_PROP}^2$	$\sigma_{PD\_PROP}^2$	
<b>Individual PK</b>	43.2	24.5	30.4				44.8		
<b>Individual PK/PD</b>	48.7	17.4	21.0	7.2	96.9	12.3	31.7	42.6	

\* In all cases Exchange algorithm (Ogungbenro, 2006, Computer Method Prog Biomed) with 0.01 step size was used

# Optimal design for individual human TGFb inhibitor model

- PK
  - Two early samples with last time at upper bound 24h (due to proportional error model)
  - reasonable CVSE on structural parameters (ka 43%); slightly larger on proportional error (45%);
- PK/PD:
  - Repetition of all three sampling times;
  - Parameter CVSEs close to or <40 with exception of IC50 (97%)

# Assessing clinically relevant designs

A number of different designs were considered

Practical designs	Efficiency [%]
[0 1 3 6 8 16 24]	90.5
[0 2 6 8 16 24]	79.9
[0 1 3 6 12 24]	80.9

Ka	CVSE [%]					kout	$\sigma^2_{PK\_PROP}$	$\sigma^2_{PD\_PROP}$
	CL	V	Imax	IC50				
56.8	14.2	18.4	5.6	118.7	16.0	29.3	39.4	
60.5	16.9	22.2	6.30	121.6	16.22	31.65	42.57	
57.5	15.11	19.28	5.98	127.6	16.22	31.65	42.58	

A variant of the first design is currently being implemented in the clinic

# Challenges in optimal design

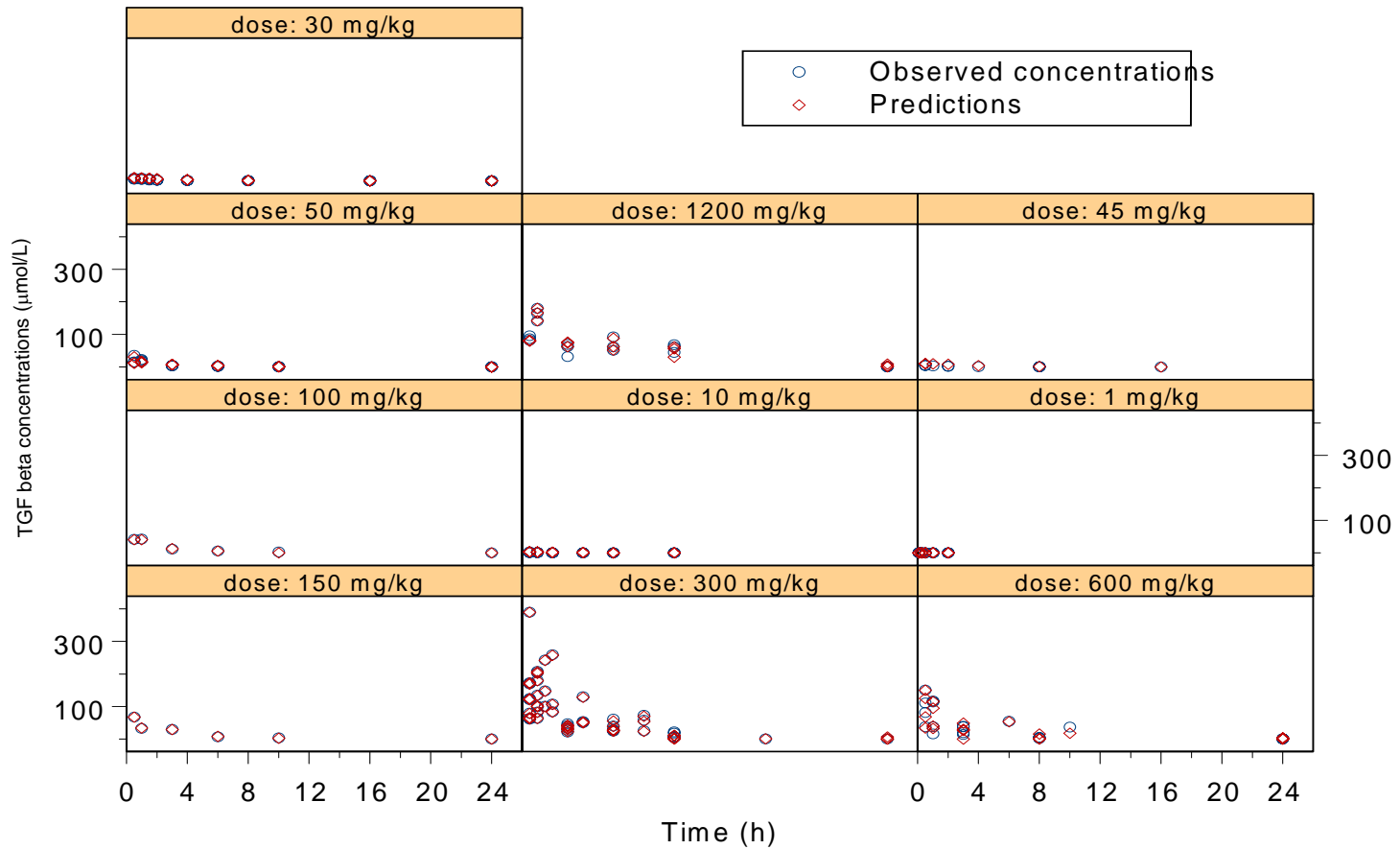
## ➤ Methodology

- Responses measured on very different time scales (clinical outcome scales in Alzheimer's disease)
  - TGFb study designed as if PK and p-SMAD inhibition measured on the same time scale (0-24h); more realistic different time frames
- sequential vs simultaneous design
- Theoretical proof/disproof of Equivalence theorem in multiresponse models

➤ **Prospective** rather than retrospective applications!

**Back up slides**

# RAT observed versus individual predicted concentrations



$$\frac{dA_1}{dt} = -kaA_1$$

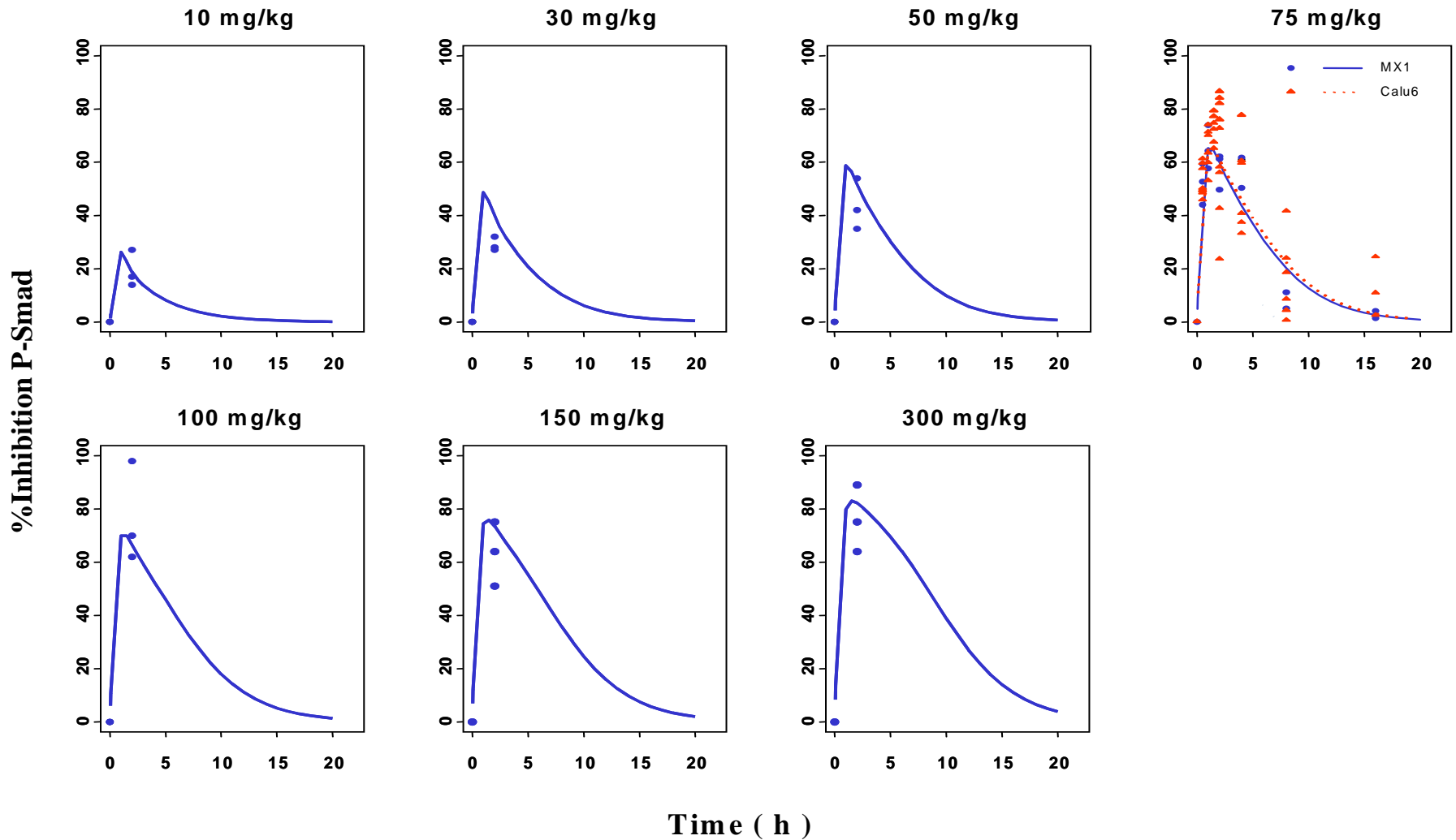
$$\frac{dA_2}{dt} = kaA_1 - \frac{CL}{V_2} A_2$$

$$\frac{dA_3}{dt} = k_{syn} \left( 1 - I_{max} \frac{A_2 / V_2}{A_2 / V_2 + IC_{50}} \right) - A_3 k_{out}$$

$$\frac{dT_S}{dt} = \frac{K_{grw1} \times T_S}{\left[ 1 + \left( \frac{K_{grw1}}{K_{grw0}} \times T_S \right)^\gamma \right]^{1/\gamma}} \times (1 - A_3)$$



# Mouse PD profiles



# Multivariate response design for an individual

$$y_{mj} = f_m(\theta, t_j) + \varepsilon_{mj}$$

$$\Sigma = \begin{pmatrix} \tau_{11} & \tau_{12} & \dots & \tau_{1M} \\ \tau_{21} & \tau_{22} & \dots & \tau_{2M} \\ \dots & \dots & \dots & \dots \\ \tau_{M1} & \tau_{M2} & \dots & \tau_{MM} \end{pmatrix} = \{\tau_{qm}\}_{1 \leq q, m \leq M}$$

$$F(\theta, \xi) = \sum_{q=1}^M \sum_{m=1}^M \left[ \frac{\partial f_q(\theta, \xi)}{\partial \theta} \right] \tau^{qm} \left[ \frac{\partial f_m(\theta, \xi)}{\partial \theta} \right]^T$$

$$\frac{\partial f_m(\theta, \xi)}{\partial \theta} = J_m(\theta, \xi) = \begin{bmatrix} \left[ \frac{\partial f_m(\theta, t_1)}{\partial \theta_1} \cdot \frac{1}{\sqrt{(\sigma_{m1}^2 + \sigma_{m2}^2 f_m(\theta, t_1)^2)}} \right] & \dots & \left[ \frac{\partial f_m(\theta, t_n)}{\partial \theta_1} \cdot \frac{1}{\sqrt{(\sigma_{m1}^2 + \sigma_{m2}^2 f_m(\theta, t_n)^2)}} \right] \\ \vdots & \ddots & \vdots \\ \left[ \frac{\partial f_m(\theta, t_1)}{\partial \theta_p} \cdot \frac{1}{\sqrt{(\sigma_{m1}^2 + \sigma_{m2}^2 f_m(\theta, t_1)^2)}} \right] & \dots & \left[ \frac{\partial f_m(\theta, t_n)}{\partial \theta_p} \cdot \frac{1}{\sqrt{(\sigma_{m1}^2 + \sigma_{m2}^2 f_m(\theta, t_n)^2)}} \right] \end{bmatrix}$$

$$\frac{\partial f_m(\theta, \xi)}{\partial \theta} = J_m(\theta, \xi) = \left\{ \frac{\partial f_m(\theta, t_j)}{\partial \theta_k} \cdot \frac{1}{\sqrt{(\sigma_{m1}^2 + \sigma_{m2}^2 f(\theta, t_j)^2)}} \right\}_{\substack{1 \leq j \leq n \\ 1 \leq k \leq p \\ 1 \leq m \leq M}}$$

# Population multivariate response design

$$y_{imj} = f_m(\theta_i, t_{ij}) + \varepsilon_{imj}$$

$$Y_i = \begin{bmatrix} y_{11} & y_{12} & \cdot & \cdot & \cdot & y_{1M} \\ y_{21} & y_{22} & \cdot & \cdot & \cdot & y_{2M} \\ \cdot & \cdot & \cdot & \cdot & \cdot & \cdot \\ \cdot & \cdot & \cdot & \cdot & \cdot & \cdot \\ y_{n1} & y_{n1} & \cdot & \cdot & \cdot & y_{nM} \end{bmatrix}$$

$$y_i = \text{vec}(Y_i) = [y'_{i1}, y'_{i2}, \dots, y'_{iM}]'$$

$$\varepsilon_i = \text{vec}(\Gamma_i) = [\eta'_{i1}, \varepsilon'_{i2}, \dots, \varepsilon'_{iM}]'$$

$$\varepsilon_i \sim MVN(0, R)$$

$$R = \begin{bmatrix} R_{11} & R_{12} & \cdot & \cdot & \cdot & R_{1M} \\ R_{21} & R_{22} & \cdot & \cdot & \cdot & R_{2M} \\ \cdot & \cdot & \cdot & \cdot & \cdot & \cdot \\ \cdot & \cdot & \cdot & \cdot & \cdot & \cdot \\ \cdot & \cdot & \cdot & \cdot & \cdot & \cdot \\ R_{M1} & R_{M2} & \cdot & \cdot & \cdot & R_{MM} \end{bmatrix}$$

$$R_{qm}(j, l) \Big|_{j=l} = \left\{ \tau_{qm} * \sqrt{(\sigma_{q1}^2 + (\sigma_{q2}^2 * f_q(\theta, t_j)^2)) * (\sigma_{m1}^2 + (\sigma_{m2}^2 * f_m(\theta, t_j)^2))} \right\}_{\substack{1 \leq q, m \leq M \\ 1 \leq j, l \leq n}}$$

$$R_{qm}(j, l) \Big|_{j \neq l} = \{0\}_{\substack{1 \leq q, m \leq M \\ 1 \leq j, l \leq n}}$$

$$\lambda = [\omega_1^2, \dots, \omega_p^2, \sigma_{11}^2, \dots, \sigma_{1M}^2, \sigma_{21}^2, \dots, \sigma_{2M}^2]$$

$$F(\Psi, \xi_i) = \left[ -\frac{\partial^2 l(\Psi, y_i)}{\partial \Psi^T \partial \Psi} \right]$$

$$y_{im} = f_m(\theta, b_i, \xi_i) + \varepsilon_{im} \cong f_m(\theta, 0, \xi_i) + \frac{\partial f_m^T(\theta, b_i, \xi_i)}{\partial b_i} \Big|_{b_i=0} b_i + \varepsilon_{im}$$

$$F(\Psi, \xi_i)_{ab} = \left\{ J_a^T V^{-1} J_b + \frac{1}{2} \text{tr} \left( \frac{\partial V}{\partial \Psi_a} V^{-1} \frac{\partial V}{\partial \Psi_b} V^{-1} \right) \right\}_{1 \leq a, b \leq (p*2+2*M)}$$

# Predicted and observed tumor growth delay

