

# Adaptive Dose Finding in Early Phase Clinical Trials Incorporating Pharmacokinetic Information

M. I. Alam, B. Bogacka and D. S. Coad

School of Mathematical Sciences  
Queen Mary  
University of London  
*m.alam@qmul.ac.uk*

June 15, 2013

# Outline

- 1 Clinical Trials
- 2 Proposed Design
  - Goals
  - Algorithm
- 3 An Example
  - PK Model
  - Dose-Response Model
  - Dose Selection Criteria
  - Stopping Rules
  - Simulations
  - Discussion
- 4 References

# Clinical Trials

Clinical trials are commonly classified into **four** phases:

- **Phase I** is the first stage of testing in humans and designed to assess safety, tolerability and pharmacokinetics (PK) of a drug.
- **Phase II** is designed to assess how well the drug works and it also monitors safety in a large group of patients.
- **Phase III** assesses the effectiveness of the drug in comparison with the current standard treatments.
- **Phase IV**, also known as post-marketing surveillance, aims to detect any rare or long-term adverse effects over a large population.

# Goals

- Recently, interest has grown in the development of dose finding methods incorporating both toxicity and efficacy as endpoints. Such trials are often seamless **phase I-II** trials.
- We introduce a new method which along with efficacy and toxicity as endpoints also considers **PK** information in dose-escalation.
- The **goal** is to develop an efficient dose finding method that exposes only a few patients to either sub-therapeutic or toxic doses.

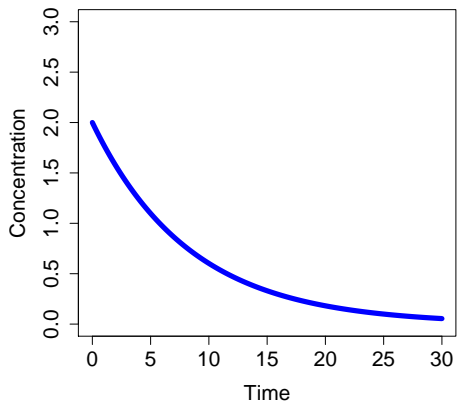


Figure 1: Concentration profile for an individual.

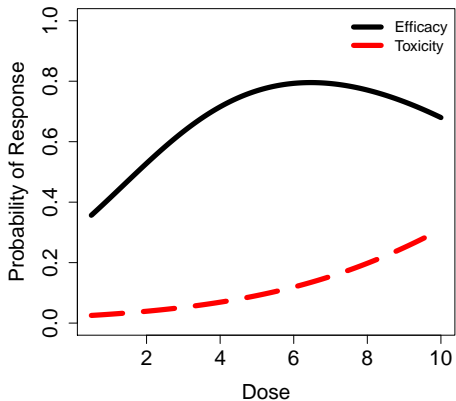


Figure 2: Dose-response curves.

# Algorithm

Let  $k$  represent the stage in a trial and set it to 1 initially. Then the algorithm proceeds as follows:

**Step 1:** Treat a cohort of size  $c$  with the **current best dose**.

**Step 2:** Obtain the **PK responses** at the locally  **$D$ -optimal** sampling time points.

**Step 3:** Observe the **dose-response outcomes**.

**Step 4:** **Estimate** PK and dose-response parameters. **Update** the dose-response curves.

**Step 5:** Select the best **dose for the next cohort** based on the chosen **criteria**.

**Step 6:** Stop the trial if the **stopping rule** is met, otherwise set  $k = k + 1$  and repeat Steps 1-5.

**Step 7:** Carry out a complete analysis of the data to recommend a dose for further studies.

# PK Model

The one-compartment PK model with bolus input and first-order elimination is

$$y_{il} = f(\boldsymbol{\theta}_i, t_{il}) + \epsilon_{il} = \frac{x}{V_i} \exp\left(-\frac{Cl_i}{V_i} t_{il}\right) + \epsilon_{il},$$

where  $i = 1, \dots, N$ ,  $l = 1, \dots, n_i$ ,  $y_{il}$  is the concentration of a drug in the blood for the  $i$ th individual observed at time  $t_{il}$ ,  $x$  is the dose received and  $\boldsymbol{\theta}_i = (V_i, Cl_i)^T$  is the vector of parameters: volume of distribution and clearance.

- **Assumptions:**

- ▶  $\boldsymbol{\theta}_i = \boldsymbol{\beta} + \mathbf{b}_i$ , where  $\boldsymbol{\beta} = (V, Cl)^T$  is the vector of mean population parameters and  $\mathbf{b}_i = (b_{V_i}, b_{Cl_i})^T$  is the vector of random effects.
  - ▶  $\mathbf{b}_i \sim N_2(\mathbf{0}, \boldsymbol{\Omega})$ , where  $\boldsymbol{\Omega}$  is a diagonal matrix with  $\sigma_1^2$  and  $\sigma_2^2$  on the diagonal.
  - ▶  $\boldsymbol{\epsilon}_i \sim N_{n_i}(\mathbf{0}, \sigma^2 \mathbf{I})$ .
- The vector of population parameters to be estimated is  $\boldsymbol{\Psi} = (V, Cl, \sigma_1^2, \sigma_2^2, \sigma^2)^T$ .
  - The **Fisher information matrix** is derived to find the population  $D$ -optimal time points.



# Dose-Response Model

- We consider a **trinomial response**  $\mathbf{Y} = (Y_0, Y_1, Y_2)^T$  for each patient, where  $Y_0$  is a **neutral** response,  $Y_1$  is an **efficacious** response and  $Y_2$  is a **toxic** response.
- The corresponding probabilities are  $\psi_0(x, \boldsymbol{\vartheta})$ ,  $\psi_1(x, \boldsymbol{\vartheta})$  and  $\psi_2(x, \boldsymbol{\vartheta})$  so that  $\psi_0(x, \boldsymbol{\vartheta}) + \psi_1(x, \boldsymbol{\vartheta}) + \psi_2(x, \boldsymbol{\vartheta}) = 1$ , where  $\boldsymbol{\vartheta}$  is the vector of dose-response parameters.
- The **continuation ratio** model of Fan and Chaloner (2004) is employed to model the responses, and is given as

$$\log \left( \frac{\psi_1(x, \boldsymbol{\vartheta})}{\psi_0(x, \boldsymbol{\vartheta})} \right) = \vartheta_1 + \vartheta_2 x$$

and

$$\log \left( \frac{\psi_2(x, \boldsymbol{\vartheta})}{1 - \psi_2(x, \boldsymbol{\vartheta})} \right) = \vartheta_3 + \vartheta_4 x,$$

where  $\boldsymbol{\vartheta} = (\vartheta_1, \vartheta_2, \vartheta_3, \vartheta_4)^T$  is the vector of parameters to be estimated.

# Dose Selection Criteria

Denote  $\hat{\boldsymbol{\vartheta}}_k = (\hat{\vartheta}_{k1}, \hat{\vartheta}_{k2}, \hat{\vartheta}_{k3}, \hat{\vartheta}_{k4})^T$ . We select the dose  $x_{k+1}$  for the next cohort of patients so that

$$x_{k+1} = \arg \max_{x \in \mathcal{X}} \psi_1(x, \hat{\boldsymbol{\vartheta}}_k),$$

subject to the conditions that

$$\psi_2(x_{k+1}, \hat{\boldsymbol{\vartheta}}_k) \leq \gamma$$

and

$$\frac{h(x_{k+1}, \hat{\boldsymbol{\beta}}_k) - AUC_{\text{target}}}{\hat{\text{SD}}(C_i|x_k)} \leq \delta,$$

where  $\gamma$  is the accepted level for the probability of toxicity and  $\delta = 1/\psi_1(x_k, \hat{\boldsymbol{\vartheta}}_k)$ . The vector of estimates of the mean population PK parameters is  $\hat{\boldsymbol{\beta}}_k$  and  $h(x, \hat{\boldsymbol{\beta}}_k)$  is the estimate of the approximated AUC at stage  $k$ . The estimate of the approximated standard deviation of AUC is denoted by  $\hat{\text{SD}}(C_i|x_k)$ .

# Stopping Rules

- Stop the trial when either of the following two happens
  - ▶ the same dose is repeated for  $r$  cohorts;
  - ▶ the trial reaches the maximum number of  $m$  cohorts.
- For early stopped trials, the **optimum dose (OD)** is defined as the dose that has been repeated  $r$  times. However, for trials that reach the maximum number of cohorts  $m$ , we carry out a complete analysis of the data, and define OD as the dose that would be allocated to cohort  $(m + 1)$  if that cohort were in the trial.

# Simulation Settings

- The **available doses** are  $\mathcal{X} = \{0.5, 1.0, \dots, 10.0\}$  and each trial starts with the lowest dose 0.5 mg/kg.
- **Four** hypothetical dose-response scenarios are investigated assuming a **single PK profile**.

Table 1: Parameters for simulating PK responses

$V$	$Cl$	$\sigma_1^2$	$\sigma_2^2$	$\sigma^2$
0.5	0.06	0.004	0.00005	0.000225

- For the initial four cohorts in each of the trials, doses are selected based on an **up-and-down** design.
- The **sampling time for PK** responses is assumed to be from 0 to 30 hours.
- Blood samples are obtained from the  $i$ th patient in each cohort of size  $c = 3$  at the  $n_i = 3$  optimal time points, obtained using the software *PFIM 3.2* (Bazzoli et al., 2010).

# Simulation Settings

- The accepted level for probability of toxicity is  $\gamma = 0.20$ .
- $AUC_{\text{target}}$  is set as the AUC at true OD in the scenario.
- Assume  $r = 6$  and  $m = 20$ .
- We employ a joint **uniform prior** distribution for  $\vartheta$  for Bayesian estimation.
- The design is not allowed to skip more than one dose level at a time during the trials when the dose level is increased.

# OD and Dose Allocation

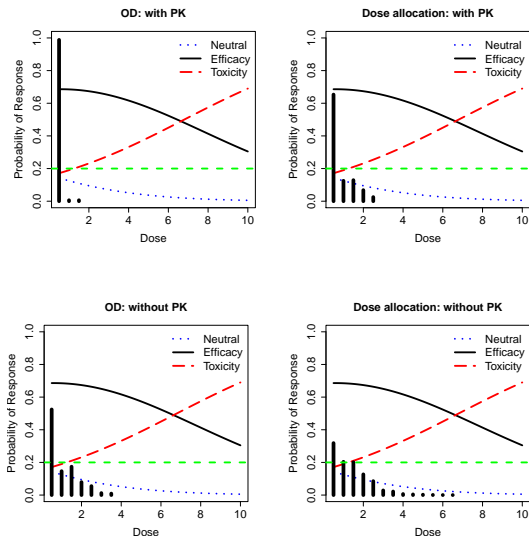


Figure 3: Scenario 1 with the OD as 0.5.

# OD and Dose Allocation

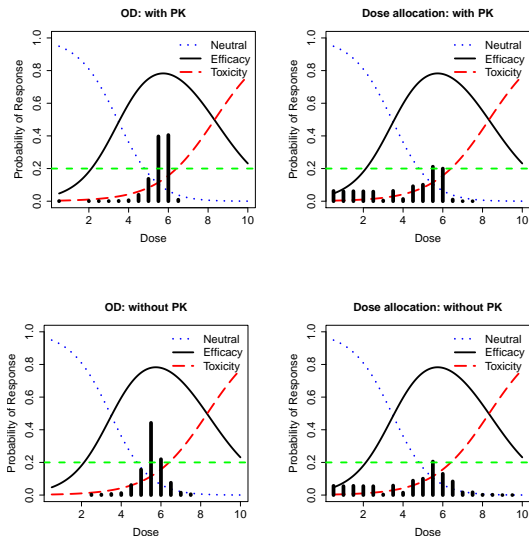


Figure 4: Scenario 2 with the OD as 5.5.

# OD and Dose Allocation

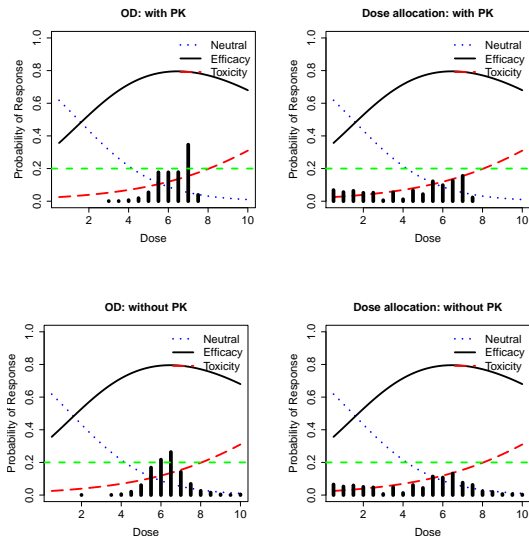


Figure 5: Scenario 3 with the OD as 6.5.



# OD and Dose Allocation

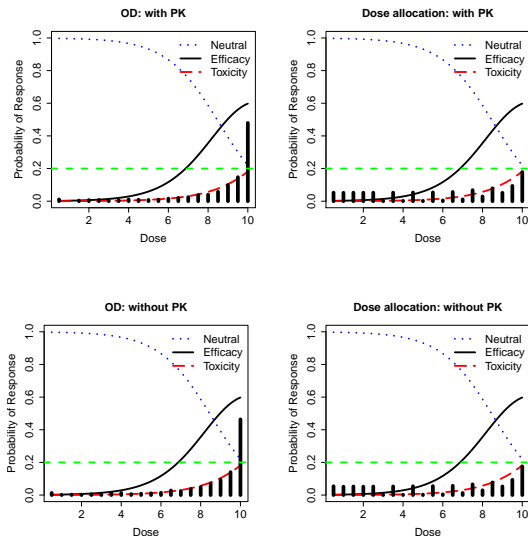


Figure 6: Scenario 4 with the OD as 10.0.

# Dose-Response Parameter Estimates

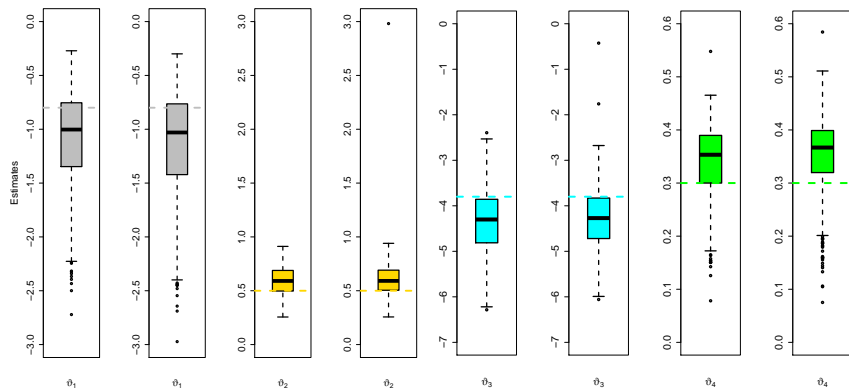


Figure 7: Box plots of the dose-response parameter estimates for [scenario 3](#) obtained from simulations. The dotted horizontal lines indicate the respective true parameter values used in the simulations.

# PK Parameter Estimates

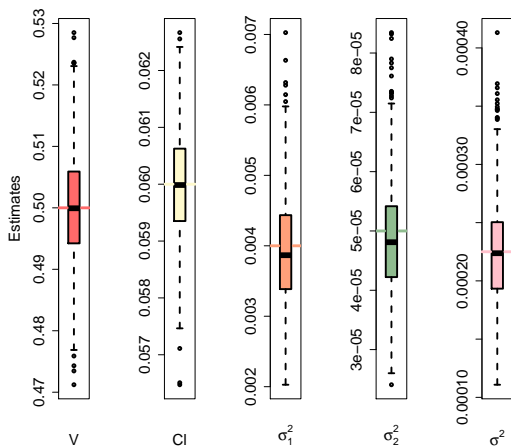


Figure 8: Box plots of the PK parameter estimates for [scenario 3](#) obtained from simulations. The dotted horizontal lines indicate the respective true parameter values used in the simulations.

# Average Cohorts Used

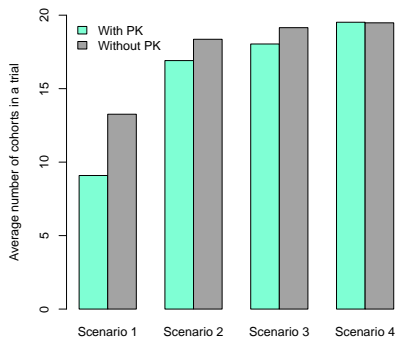


Figure 9: Average number of cohorts used in different scenarios by two different dose allocation scheme.

# Discussion

- The presented design is conceptually similar to that of Zhang et al. (2006), but their design does not incorporate PK responses.
- The new design has been found to **limit overdosing** by a considerable amount depending on the location of the OD in the scenario.
- The OD has also been identified **more accurately**.
- The design also **assigns** most of the patients to the **most relevant doses** throughout the trials.
- **Small bias and mean square error** of the PK parameter estimates have been found, as the  $D$ -criterion was used.
- The bias and mean square error of most of the dose-response parameter estimates from the PK guided approach are slightly smaller than that of the other approach.
- The design is efficient and ethical.

# References

- Bazzoli, C., T. T. Nguyen, A. Dubois, E. Retout, S. Comets, and F. Mentré (2010). *PFIM 3.2 User Guide*. Université Paris Diderot and INSERM.
- Fan, S. K. and K. Chaloner (2004). Optimal designs and limiting optimal designs for a trinomial response. *Journal of Statistical Planning and Inference* 126(1), 347–360.
- Zhang, W., D. J. Sargent, and S. Mandrekar (2006). An adaptive dose-finding design incorporating both toxicity and efficacy. *Statistics in Medicine* 25(14), 2365–2383.

Thank you